

Exercise: Heuristic for assessing applicability of PCA

(Source: (?), Q9.8). Let the empirical covariance matrix Σ have eigenvalues $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_d > 0$. Explain why the variance of the eigenvalues, $\sigma^2 = \frac{1}{d} \sum_{i=1}^d (\lambda_i - \bar{\lambda})^2$ is a good measure of whether or not PCA would be useful for analysing the data (the higher the value of σ^2 the more useful PCA).